Raman bands in the low-energy region of the spectrum of crystals are attributed to so-called external lattice vibrational modes. The Raman bands from these external vibrational modes (low-energy phonons) are very sensitive to crystal structure and orientation with respect to the incident laser polarization and to molecular interactions within the crystal. The low-energy vibrational modes of many organic molecular crystals have very high Raman scattering cross-sections. Raman spectra and images of low-energy phonons in two-dimensional (2D) crystals such as few-layer MoS$_2$ reveal spatial variations in the solid-state structure that are not evident in the higher-energy bands.

David Tuschel

In chemistry courses we learn about Raman scattering through the interaction of light with molecules. A molecule, initially in the ground state, interacts with an incident photon driving the molecule to a virtual energy state whereupon it drops to the first excited vibrational state and emits a photon (Stokes Raman scattering). The energy difference between the incident and scattered photons is equal to the energy difference between the ground and first excited vibrational states. If the molecule initially had been in the first excited vibrational state and ended in the ground state, a quantum of energy would have been transferred from the molecule to the scattered photon and its energy would have been greater than that of the incident photon (anti-Stokes Raman scattering). Hence, one can observe the Raman spectrum at either longer (Stokes) or shorter (anti-Stokes) wavelengths relative to that of the incident monochromatic laser beam.

When dealing with gases or liquids it is appropriate to speak of the interaction of a photon with individual molecules. However, very often we deal with solid-state materials for which there may be no molecular species—for example, TiO$_2$, Si, C (graphene or diamond), and CaCO$_3$. Raman spectroscopy of solid-state materials involves the inelastic scattering of light by phonons, quanta that have the energy of lattice vibrations. The Stokes and anti-Stokes Raman scattering consist of the generation or annihilation of a phonon in the solid, respectively. In crystalline materials, the phonons can be understood as lattice vibrational modes whether the crystal is a covalent or ionic solid or a molecular crystal such as TiO$_2$, BaF$_2$, or H$_2$O (ice), respectively.

When speaking of Raman spectra of solid-state materials, some spectroscopists will describe certain bands as phonons and others as molecular vibrations. Strictly speaking, this is not correct; all of the bands in a Raman spectrum of a solid arise from phonons. A more appropriate distinction is to speak of external and internal lattice vibrational modes when speaking of solid-state Raman band assignments, particularly for molecular crystals (1). An external vibration can be thought of as the collective motion of molecules as a whole, such as whole water molecules moving collectively in an ice crystal. Some low-energy Raman bands are a result of shear or interlayer breathing modes of the crystal layers. The shear modes can be pictured as atomic or molecular lay-
ers moving antiparallel to each other within their planes whereas the breathing modes involve the layers moving away from and toward each other. The external vibrations are generally of low energy and of course would be absent from the liquid or gas spectrum of the material because of the absence of long-range translational symmetry present in a crystal. The internal vibrational modes arise from the coupling through the crystal of the local vibrational modes observed for the molecular species. We can think of these types of phonons as collective local modes modified through coupling with other molecules in the crystal and affected by their arrangement in the lattice. Their Raman shifts are often similar but not identical to those of the molecular (liquid or gas) spectrum.

As you may expect, the external vibrational modes or low-energy phonons are very sensitive to crystal structure. That is why the external modes have proven so useful in the pharmaceutical industry for the characterization and screening of polymorphs. In addition, Raman spectra of low-energy phonons are dependent upon the crystal orientation with respect to the incident laser polarization. Perhaps less well known is the sensitivity of the external modes to molecular interactions such as hydrogen bonding or even the weaker van der Waals forces between molecular or atomic layers. Here, we discuss those aspects of chemical bonding and structure that affect the Raman spectroscopy of low-energy phonons and demonstrate the practicality of imaging them for the characterization of 2D crystals.

**Stokes, Anti-Stokes, and Temperature**

Sulfur is well known for its strong Raman scattering and the low-energy phonons that can be detected if one can get close enough to the laser line. Two spectra of sulfur acquired from different grains from the same sample source are shown in Figure 1. The use of a 532-nm laser with a very narrow line (highly monochromatic) in conjunction with a laser line rejec-

![Figure 1: Raman spectra of different grains of sulfur demonstrating Raman scattering from low-energy phonons and how crystal orientation affects the relative intensities.](image1)

![Figure 2: Raman spectra of different grains of aspirin demonstrating Raman scattering from low-energy phonons and how crystal orientation affects the relative intensities.](image2)

![Figure 3: Raman spectra of different grains of procaine demonstrating the signal strength of external vibrational modes and how crystal orientation affects the relative intensities.](image3)
The lowest energy band detected in the sulfur spectrum is at 28.1 cm\(^{-1}\), much lower than the conventional laser line cutoff. There are several things to notice about the sulfur spectra in Figure 1. The first is that the signal strengths of the anti-Stokes Raman bands grow progressively weaker with greater Raman shift. For example, the strong bands at 219.3 and 472.8 cm\(^{-1}\) in the Stokes spectrum are considerably weaker on the anti-Stokes side. This is because the population of the first excited vibrational state is dependent on the temperature and the difference in energy between the ground and first excited vibrational state. Consequently, the higher the energy of the first excited vibrational state or phonon, the lower the population of that state and the weaker the anti-Stokes Raman scattering will be.

In fact, the ratio of the anti-Stokes to Stokes Raman scattering is entirely dependent on the energy of the vibrational transition and the temperature. The following expression describes the mathematical relationship of the anti-Stokes and Stokes Raman scattering signal strength with temperature and the energy of the vibrational transition

\[
\frac{I_{AS}}{I_{S}} = \frac{\left(\nu_l + \nu_v\right)^4}{\left(\nu_l - \nu_v\right)^4} \ e^{\left(h\nu_v/kT\right)} \quad [1]
\]

where \(I_{AS}\) is the anti-Stokes signal strength, \(I_{S}\) is the Stokes signal strength, \(\nu_l\) is the laser frequency expressed in terms of wavenumbers (reciprocal centimeters), \(\nu_v\) is the vibrational mode frequency, \(h\) is Planck's constant, \(k\) is Boltzmann's constant, and \(T\) is the temperature (2). What follows from this expression is that the temperature of a substance can be determined by measuring the Stokes and anti-Stokes Raman scattering. Any pair of anti-Stokes and Stokes Raman bands from the spectrum should suffice because their peak positions are easily identified. However, of those measurable components in the equation above, the Raman signal strength is what most affects the accuracy and precision of temperatures that are derived from the Raman spectrum. Consequently, as we can clearly see from the spectra in Figure 1, the lower the energy of the Raman band the stronger the anti-Stokes signal will be. So, the best anti-Stokes signal-to-noise for temperature determination will be obtained by using bands at the lowest Raman shifts, that is, low-energy phonons.

### Crystal Orientation and Molecular Interactions

Another important observation to be made of the spectra in Figure 1 is that the relative intensities are significantly different. The spectra were acquired from different sulfur grains oriented differently with respect to the incident laser polarization. No Raman polarization analyzer was used and yet we see substantial spectral differences with crystal orientation. Of course, the low-energy phonons follow the same Raman polarization selection rules that govern the higher energy phonons or internal vibrational modes. The effects of laser polarization with respect to crystal orientation are further demonstrated in the Raman spectra acquired from aspirin and procaine grains shown in Figures 2 and 3, respectively. Both compounds are pharmaceutical ingredients; procaine (C\(_{13}\)H\(_{20}\)N\(_2\)O\(_2\)) is a compound used primarily as a topical anesthetic. The aspirin and procaine spectra were obtained by focusing the 532-nm laser beam with an Olympus 100\(\times\) microscope objective on different grains from the same source. A cursory examination of the aspirin spectra might lead the uninitiated to incorrectly conclude that the spectra were acquired from different compounds when in fact the grains are simply oriented differently. Regarding the procaine, note how strong the Raman scattering of the external phonons is, specifically the bands at 23.5, 31.0, and 34.7 cm\(^{-1}\). It is well known that the low-energy phonon modes of many organic molecular crystals have very high Raman scattering cross-sections. That is one reason why the pharmaceutical industry finds this region of the Raman spectrum so useful for the differentiation of polymorphs. However, the Raman spectra of procaine very effectively demonstrate the sensitivity of crystal orientation to incident laser polarization, which must be accounted for when using Raman spectroscopy for polymorph characterization. The spectra of sulfur, aspirin, and procaine acquired at different crystal orientation...
tions with respect to the incident laser polarization should impress upon the spectroscopist that care must be taken in interpreting low-energy Raman spectra of crystalline grains, particularly if one is using that portion of the Raman spectrum to characterize or differentiate polymorphs. Recalling the previously discussed temperature measurements, the procaine spectra demonstrate the value of using Stokes and anti-Stokes Raman bands of low-energy phonons to determine temperature. The signal-to-noise of the anti-Stokes scattering is very strong, thereby yielding more-accurate temperatures.

In the introduction we stated that the external vibrational modes are particularly sensitive to molecular interactions and interlayer van der Waals forces. Here we demonstrate that claim through the Raman spectra of cystine and the amino acid cysteine shown in Figure 4. Cystine is the oxidized form of cysteine wherein “the thiol groups of two molecules of cysteine have been oxidized to a disulfide group to provide a covalent cross-linkage between them” (3). Both spectra were acquired from individual grains taken from reagent bottles of the crystalline forms of cystine and cysteine. In spite of the fact that the two compounds are compositionally similar, the low-energy Raman spectra are remarkably different. The cystine Raman bands are very sharp with two bands at 10.2 and 14.9 cm\(^{-1}\) fully resolved. In contrast, the Raman spectrum of cysteine has low-energy bands that are much broader compared to those of cystine. The region from 20 to approximately 130 cm\(^{-1}\) in the cysteine spectrum manifests Raman scattering with no baseline and broad maxima at the positions labeled on the spectrum. The breadth of the low-energy Raman bands indicates strong molecular interactions within the cysteine crystal. In contrast, the cystine Raman spectrum manifests very sharp peaks thereby indicating very weak molecular interactions.

Even though the molecular interactions in a crystalline form are strong and the Raman bands are broad, the spectrum will still manifest a dependence on crystal orientation with re-
Raman Spectroscopy of Few-Layer MoS$_2$ Low-Energy Phonons

Thus far, the spectra that we have examined have been of bulk crystals. Here we find that Raman spectra of low-energy phonons in so-called two-dimensional (2D) crystals such as few-layer MoS$_2$ can be quite revealing about the solid-state structure. The low-energy band structure of 2D crystals vary far more with solid-state structures than do the higher-energy optical phonons. Raman spectra of bulk MoS$_2$ and a few-layer sample acquired with 532 nm excitation are shown in Figure 6. The bulk spectrum consists of the single $E^{2g}_{2g}$ band at 32.8 cm$^{-1}$. However, the few-layer MoS$_2$ spectrum consists of the $E^{2g}_{2g}$ band at 32.0 cm$^{-1}$, three weak bands just below 30 cm$^{-1}$, a strong band at 9.0 cm$^{-1}$, and a Si substrate band at 5.1 cm$^{-1}$. Examination of multiple few-layer flakes as well as different positions on a single flake reveals a variety of low-energy Raman bands as shown in Figure 7. Note that the $E^{2g}_{2g}$ band at approximately 32 cm$^{-1}$ does vary slightly in position and strength.
but not as significantly as the bands below 30 cm\(^{-1}\). The analysis and interpretation of the low-energy interlayer breathing and shear modes of few-layer MoS\(_2\) have been rigorously studied (5–7). For a more detailed discussion of Raman spectroscopy and imaging of higher energy Raman bands of few-layer MoS\(_2\), consult the March 2015 issue of Spectroscopy (8).

A clear pattern emerges between the appearance of low-energy phonon modes in the Raman spectra of few-layer MoS\(_2\) and the location on or color of a particular flake. Spectra acquired from the edge and purple sections of a few-layer MoS\(_2\) flake are shown in Figure 8. Note the low-energy bands below the \(E_{2g}\) band and their varied Raman shifts at the different positions on the flake; none of these bands appear in the bulk spectrum of MoS\(_2\). Furthermore, even when the band structures appear similar as in the spectra from positions (b) and (c), the low-energy phonon peak positions are not identical except for the \(E_{2g}\) and Si substrate (4.8 cm\(^{-1}\)) bands. The peak positions below the \(E_{2g}\) band differ by approximately 1 cm\(^{-1}\) in the spectra from locations (b) and (c). The low-energy Raman spectra of few-layer exfoliated MoS\(_2\) flakes reveal a solid-state structural heterogeneity that is not observed in the higher energy phonons.

The edges or perimeters of few-layer MoS\(_2\) flakes often consist of small (several micrometers) extensions with varying shades of purple and very different low-energy Raman spectra. A reflected light image of one such few-layer flake is shown in Figure 9. The colors of these small extensions of the flake range from deep blue to purple. Raman spectra were acquired at positions labeled (a) through (d) and they are shown in Figure 10. Here, again, we see small shifts in the \(E_{2g}\) band but the number and positions of the bands at Raman shifts lower than 32 cm\(^{-1}\) vary more significantly with position. The interpretation of the low-energy Raman spectra in conjunction with the colors of whole few-layer flakes and these edge features should be an intriguing and important area of study. In particular, the application of atomic force microscopy in conjunction with reflected light optical microscopy and low-energy Raman spectroscopy and imaging would be helpful in possibly correlating the color and Raman band structure to the number of MoS\(_2\) layers.

Raman Imaging of Few-Layer MoS\(_2\) Low-Energy Phonons

Now that we’ve seen the rich variety of spectra uncovered below the \(E_{2g}\) band, with respect to position it seems reasonable to map the few-layer MoS\(_2\) flakes to render Raman images of the low-energy phonons. A collection of data from a few-layer MoS\(_2\) flake is shown in Figure 11. The Raman data were acquired using 532-nm excitation and a 100× Olympus objective and by moving the stage in 200-nm increments over an area of approximately 55 \(\mu\)m \(\times\) 30 \(\mu\)m. The Raman images in the lower left, lower right, and upper right frames are rendered using the green color brackets to capture the \(A_{1g}\) (not shown), \(E_{2g}\), and 29 cm\(^{-1}\) bands, respectively. The plot on the upper left consists of all of the Raman spectra acquired over the image area. The red color brackets (not shown) surrounded the 520 cm\(^{-1}\) band and so the red color in the Raman images corresponds to the Si substrate. Of course, the \(A_{1g}\), \(E_{2g}\), and 29 cm\(^{-1}\) band images of the few-layer MoS\(_2\) appear quite similar; however, there are some subtle but important differences among the three images. For example, observe and compare that portion of the images pointed out by the yellow arrows. Note that in the \(A_{1g}\) image the area appears somewhat fuzzy green and the red substrate is partially visible, perhaps indicating a thin layer of MoS\(_2\). That same area in the \(E_{2g}\) image appears completely red suggesting the absence of MoS\(_2\), at that location based on the \(E_{2g}\) image alone. However, the 29 cm\(^{-1}\) band image shows that area to be among the brightest green, thereby confirming the presence of MoS\(_2\). The variation of the green contrast among the different images may indicate a spatial variation of thickness within individual flakes. The important takeaway point from these images is that a Raman image of one peak position alone is insufficient to adequately reveal the spatially varying solid-state structure of the few-layer MoS\(_2\) flakes.

Another collection of data from a few-layer MoS\(_2\) flake is shown in Figure 12. Here again, the Raman data were acquired using 532-nm excitation and a 100× Olympus objective and by moving the stage in 200-nm increments over an area of approximately 12 \(\mu\)m \(\times\) 12 \(\mu\)m. A reflected white light
The differences between the $A_{1g}$ and $E_{2g}$ Raman images reminds us that depending upon the complexity of the material, rendering an image based on a single band can sometimes provide only a single perspective and not the whole picture. In fact, images of the same flake based on the low-energy phonon modes between 15 cm$^{-1}$ and 31 cm$^{-1}$ reveal just how heterogeneous this few-layer flake is despite its appearance in the $A_{1g}$ and reflected white light images. A series of Raman images at 31, 29, 28, 23, and 15 cm$^{-1}$ of this same few-layer flake is shown in Figure 13. All of the images are on different intensity scales, normalized to the maximum and minimum signal strength of that particular Raman band. Note how significantly different the images appear even though they are separated by only a small Raman shift. At 29 cm$^{-1}$ a portion of the top bright region in the 31 cm$^{-1}$ Raman image has grown dim and “holes” revealing the red Si substrate begin to appear on the right and bottom portions of the flake. At 28 cm$^{-1}$ the top formerly bright green region has grown dark, the holes revealing the red Si substrate have grown clearer, and the rest of the flake is uniformly bright green. Next, the 23 cm$^{-1}$ image appears to be almost the inverse of that at 28 cm$^{-1}$; the formerly red holes now appear the brightest green because of MoS$_2$ Raman scattering. Finally, the 15 cm$^{-1}$ Raman image shows strong contrast with the top portion of the flake appearing bright green and the remainder very dim because of the weakness or absence of scattering at that Raman shift.

Continuing with our theme that multiple perspectives provide a more complete image, another collection of data from a few-layer MoS$_2$ flake is shown in Figure 14. The Raman data were acquired using 532-nm excitation and a 100× Olympus objective and by moving the stage in 200-nm increments over an area of approximately 11 µm × 11 µm. A reflected white light image of the flake appears in the lower right-hand corner and Raman $A_{1g}$ and $E_{2g}$ images of the same area appear in the lower left-hand and upper right-hand corners, respec-
tively. The bright red areas indicate a bare Si substrate. The plot on the upper left consists of all of the Raman spectra acquired over the image area. The Raman images in the lower left and upper right frames are rendered using the green color brackets to capture the \(A_{1g}\) (not shown) and \(E^{2g}\) bands, respectively. We see that once again the \(A_{1g}\) and \(E^{2g}\) images are similar but not identical. The green contrast of the strongest to the weakest Raman scattering in the two images are different; the \(A_{1g}\) Raman image appears relatively more uniform than that of the \(E^{2g}\) image. Interestingly, both images show dark lines (weak Raman scattering) where two near vertical white lines appear in the reflected white light image. Comparison of the \(A_{1g}\) and \(E^{2g}\) images informs us that the few-layer MoS\(_2\) solid-state structure is not uniform. If the flake were to be uniformly oriented over an area of approximately 11 \(\mu m\) \(\times\) 15 \(\mu m\). A reflected white light image of the flake appears in the lower right-hand corner and Raman \(A_{1g}\) and 8 \(cm^{-1}\) images of the same area appear in the lower left-hand and upper right-hand corners, respectively. The bright red areas indicate a bare Si substrate. The plot in the upper left consists of all of the Raman spectra acquired over the image area. The Raman images in the lower left and upper right frames are rendered using the green color brackets to capture the \(A_{1g}\) and 8 \(cm^{-1}\) bands, respectively. The \(A_{1g}\) image bears what we may call an inverse correspondence to the reflected white light image, that is, the brighter and darker areas in the reflected light image manifest weak and strong Raman scattering in the \(A_{1g}\) image, respectively. The inverse correspondence of the reflected light and \(A_{1g}\) and \(E^{2g}\) images is really quite striking and typical of all of the \(A_{1g}\) and \(E^{2g}\) images that we have acquired of few-layer MoS\(_2\) exfoliated flakes.

\[\text{Figure 14: Raman images of few-layer MoS}_2\text{ flake obtained with 532-nm excitation. Red corresponds to the substrate Si and the green intensities correspond to the spatially varying strength of the Raman bands at approximately 408 and 31 cm}^{-1}.\]

\[\text{Figure 15: A series of Raman images at 31, 30, 28, 23, 19, and 8 cm}^{-1}\text{ of the same few-layer flake shown in Figure 14. All of the images are on different intensity scales, normalized to the maximum and minimum signal strength of that particular Raman band.}\]
crystalline grains, particularly if one is using that portion of the Raman spectrum to characterize or differentiate polymorphs. The sensitivity of the external modes to molecular interactions, such as hydrogen bonding or even the weaker van der Waals forces, between molecular or atomic layers was demonstrated.

There is a clear pattern between the appearance of low-energy phonon modes in the Raman spectra of few-layer MoS$_2$ and the location on or color of a particular flake. The interpretation of the low-energy Raman spectra in conjunction with the colors of whole few-layer flakes and the edge features should be an intriguing and important area of study. In particular, the application of atomic force microscopy in conjunction with reflected light optical microscopy and low-energy Raman spectroscopy and imaging would be helpful in possibly correlating the color and Raman band structure to the number of MoS$_2$ layers.

We discussed the Raman spectroscopy of low-energy phonons and demonstrated the practicality of imaging them for the characterization of 2D crystals. The important takeaway point from these images is that a Raman image of one peak position alone is insufficient to adequately reveal the spatially varying solid-state structure of the few-layer MoS$_2$ flakes. Images rendered from the spatially varying signal strengths of the high- and low-energy phonon modes of few-layer MoS$_2$ correspond to the internal vibrational modes and the shear and interlayer breathing modes, respectively. A single Raman image of any of these modes is insufficient to reveal the solid state structure. Viewing Raman images of all the modes allows one to form a more complete understanding of 2D crystal structures such as few-layer MoS$_2$.

**Conclusions**

Raman spectra of low-energy phonons are dependent on the crystal orientation with respect to the incident laser polarization. The spectra of sulfur, aspirin, and procaine acquired at different crystal orientations with respect to the incident laser polarization should impress upon the spectroscopist that care must be taken in interpreting low-energy Raman spectra of crystalline grains, particularly if one is using that portion of the Raman spectrum to characterize or differentiate polymorphs. The sensitivity of the external modes to molecular interactions, such as hydrogen bonding or even the weaker van der Waals forces, between molecular or atomic layers was demonstrated.

There is a clear pattern between the appearance of low-energy phonon modes in the Raman spectra of few-layer MoS$_2$ and the location on or color of a particular flake. The interpretation of the low-energy Raman spectra in conjunction with the colors of whole few-layer flakes and the edge features should be an intriguing and important area of study. In particular, the application of atomic force microscopy in conjunction with reflected light optical microscopy and low-energy Raman spectroscopy and imaging would be helpful in possibly correlating the color and Raman band structure to the number of MoS$_2$ layers.

We discussed the Raman spectroscopy of low-energy phonons and demonstrated the practicality of imaging them for the characterization of 2D crystals. The important takeaway point from these images is that a Raman image of one peak position alone is insufficient to adequately reveal the spatially varying solid-state structure of the few-layer MoS$_2$ flakes. Images rendered from the spatially varying signal strengths of the high- and low-energy phonon modes of few-layer MoS$_2$ correspond to the internal vibrational modes and the shear and interlayer breathing modes, respectively. A single Raman image of any of these modes is insufficient to reveal the solid state structure. Viewing Raman images of all the modes allows one to form a more complete understanding of 2D crystal structures such as few-layer MoS$_2$.

**References**


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**Figure 16:** Raman images of few-layer MoS$_2$ flakes obtained with 532-nm excitation. Red corresponds to the substrate Si and the green intensities correspond to the spatially varying strength of the Raman bands at approximately 408 and 8 cm$^{-1}$.

The 8 cm$^{-1}$ Raman image also shows an inverse correspondence, but not to the contrast level of the A$_{1g}$ image. Nevertheless, the darkest areas of the reflected light image do correspond to the brightest regions in the 8 cm$^{-1}$ Raman image.

Images of the high- and low-energy MoS$_2$. Raman bands correspond to the internal vibrational modes and the shear and interlayer breathing modes, respectively. Altogether, they provide multiple perspectives to form a more complete image of 2D crystals such as few-layer MoS$_2$.